1. Let $x_0 = 1$ and consider the sequence $x_n$ given by the formula

$$x_n = \frac{2}{3} x_{n-1} + \frac{1}{x_{n-1}} \quad n = 1, 2, 3, \cdots$$

Use Maple to compute the first 15 terms of the sequence and make a conjecture about the limit of the sequence.

**Extra Credit:** Prove your conjecture.

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**Problem 2. Power series approximation**

(a) Find the power series representation centered at 0 for the function

$$f(x) = \frac{\ln(x^2 + 1)}{x^2}$$

(b) Graph $f$ and the tenth-degree Taylor polynomial $P_{10}(x)$ for $f$ on the same coordinate system.

(c) Consider $F(x)$ and $G(x)$ defined below:

$$F(x) = \int_0^x \frac{\ln(t^2 + 1)}{t^2} \, dt \quad \text{and} \quad G(x) = \int_0^x P_{10}(t) \, dt$$

Evaluate $F(0.25)$, $F(0.5)$, $G(0.25)$, $G(0.5)$, and explain the relationship between these values.